

$$\frac{d}{dt}(x_0 e^{at}) = ax_0 e^{at} = a(x_0 e^{at}) = ax$$